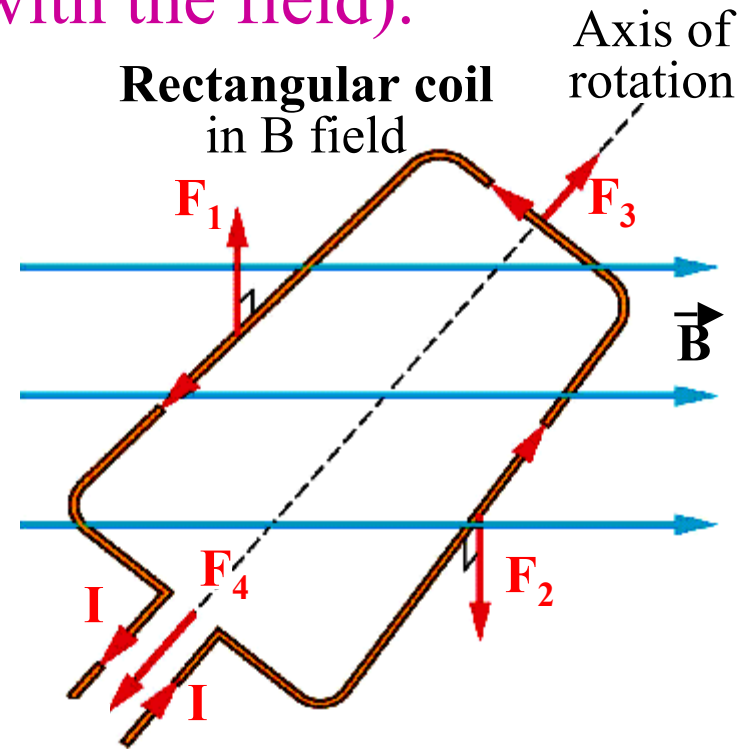


Recap: Electric Motor

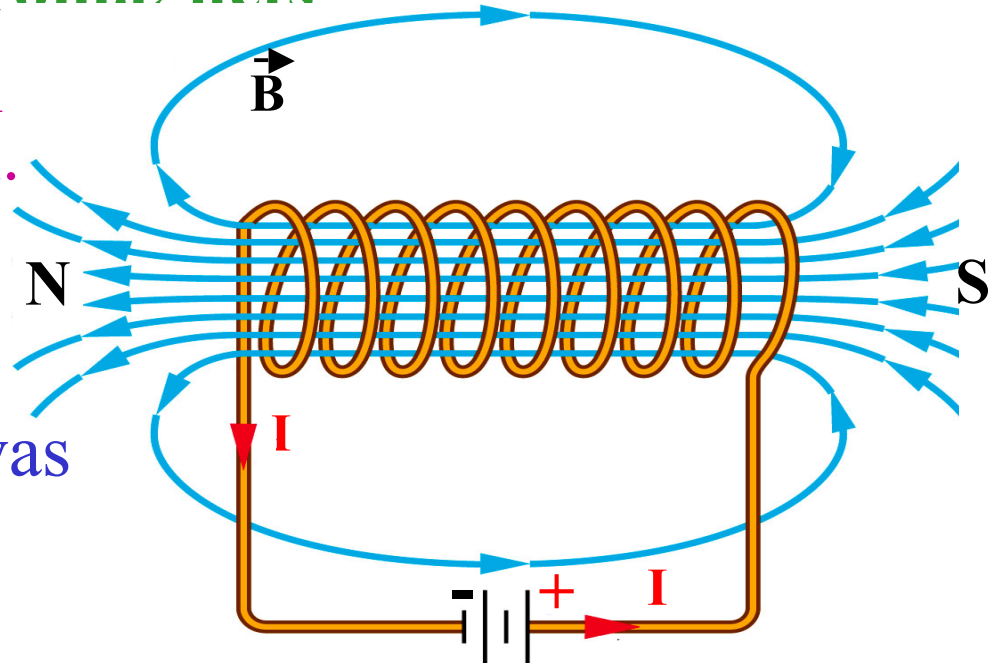
- If we place a **current loop** in an **external magnetic field**, it will experience a **torque**.
- This **torque** is the **same force** a **bar magnet** would **experience** (if not initially aligned with the field).
- Using **Right Hand rule** the forces ($F = B \cdot I \cdot l$) create:
 - F_1 and F_2 combine to produce a **torque**.
 - F_4 and F_3 produce **no torque** about the **axis of rotation**.
- Forces F_1 and F_2 will **rotate** loop until it is **perpendicular** to magnetic field (i.e. vertical in figure).
- To keep **coil turning** in an **electric motor** must **reverse** **current** direction **every $\frac{1}{2}$ cycle**.
- **AC current** is **well suited** for operating electric motors.
- In a DC motor need to use a “split ring” or “**commutator**” to reverse current.



- **Electric motors** (AC and DC) are very common:
Magnitude of torque is proportional to **current** flowing.
 Uses: car starter motor; vacuum cleaners; current meters
- **AC motors** run at a **fixed speed**.
- **DC motors** have **adjustable speed** (depending on applied voltage).

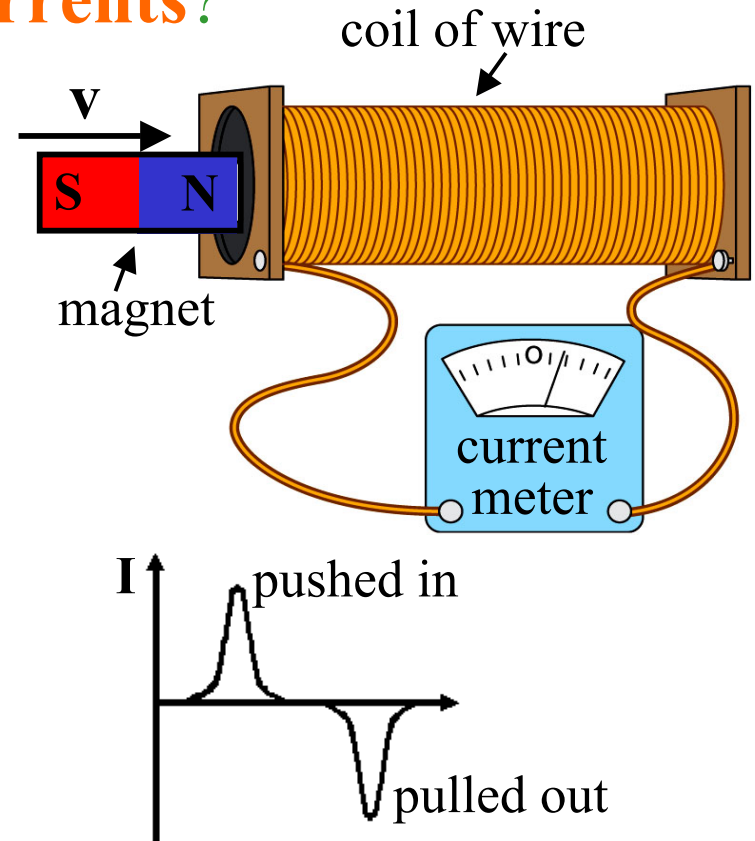
Electromagnets

- If we take a **single loop** and **extend** it into a **coil of wire** we can create a **powerful electromagnets**
- **Magnetic field** proportional to **number of turns** on coil.
- If add iron/steel core field **strength enhanced**.
- Ampere suggested **source of magnetism** in materials was **current loops** – **alignments** of “**atomic loops**” gives a **permanent magnet**.



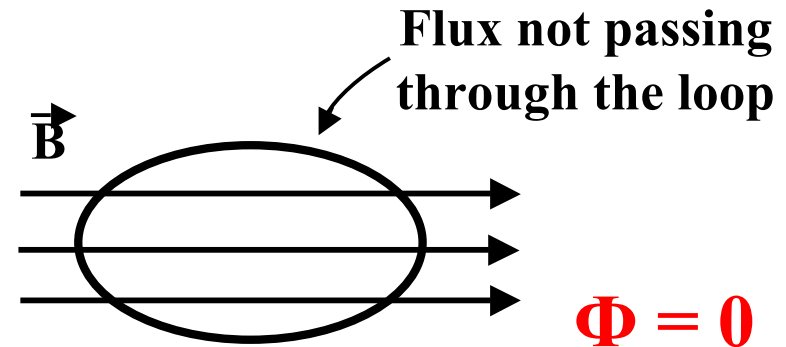
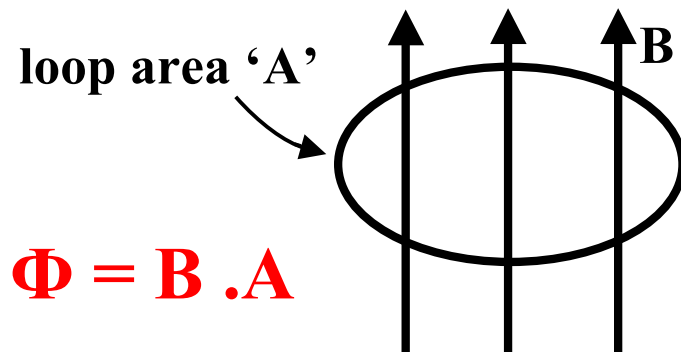
Electromagnetic Induction

- An electric current produces a magnetic field **but** can **magnetic field** produce **electric currents**?
 - Magnet moved in and out of wire coil.
 - **Michael Faraday** (U.K.) discovered that when **magnet** is **moved** in /out of a core a **current** was **briefly induced**.
 - **Direction** of current **depended** on **direction** (in/ out) of magnet.
 - When **magnet stationary** **no** **current** is **induced**.
 - **Strength** of **deflection** depended on **number of turns** on coil and on **rate of motion** of the magnet.
- Result:** Current induced in coil when magnetic field passing through coil changes.



Magnetic Flux

- Number of **magnetic field lines** passing through a **given area** (usually area of loop).



Maximum flux is obtained when **field lines** pass through circuit **perpendicular** to coil.

If **field lines parallel** to circuit plane, the **flux = 0** as **no** field lines pass through coil.

- ❖ **Faraday's Law:** A voltage is **induced** in a circuit when there is a **changing magnetic flux** in circuit.

$$\varepsilon = \frac{\Delta\Phi}{t}$$

(electromagnetic induction)

- Induced voltage 'ε' equals rate of change of flux.**

- $\Delta\Phi$ is **change** in flux
- The **more rapidly** the flux changes, the larger the induced voltage (i.e. larger meter swing).
- As magnetic **flux passes** through **each loop** in coil the total flux,

$$\Phi = N . B . A$$

- Thus the **more turns** of wire, the **larger** the **induced voltage**.

Example: Determine induced voltage in a coil of 100 turns and coil area of 0.05 m^2 , when a flux of 0.5 T (passing through coil) is reduced to zero in 0.25 sec .

$$\Phi = N . B . A = 100 \times 0.5 \times 0.05$$

$$\Phi = 2.5 \text{ T} . \text{m}^2$$

$$N = 100 \text{ turns}$$

$$B = 0.5 \text{ T}$$

$$A = 0.05 \text{ m}^2$$

$$T = 0.2 \text{ s}$$

Induced voltage:

$$\varepsilon = \frac{\Delta\Phi}{t} = \frac{2.5 - 0}{0.25} = 10 \text{ v}$$

- **Question:** What is the direction of induced current?

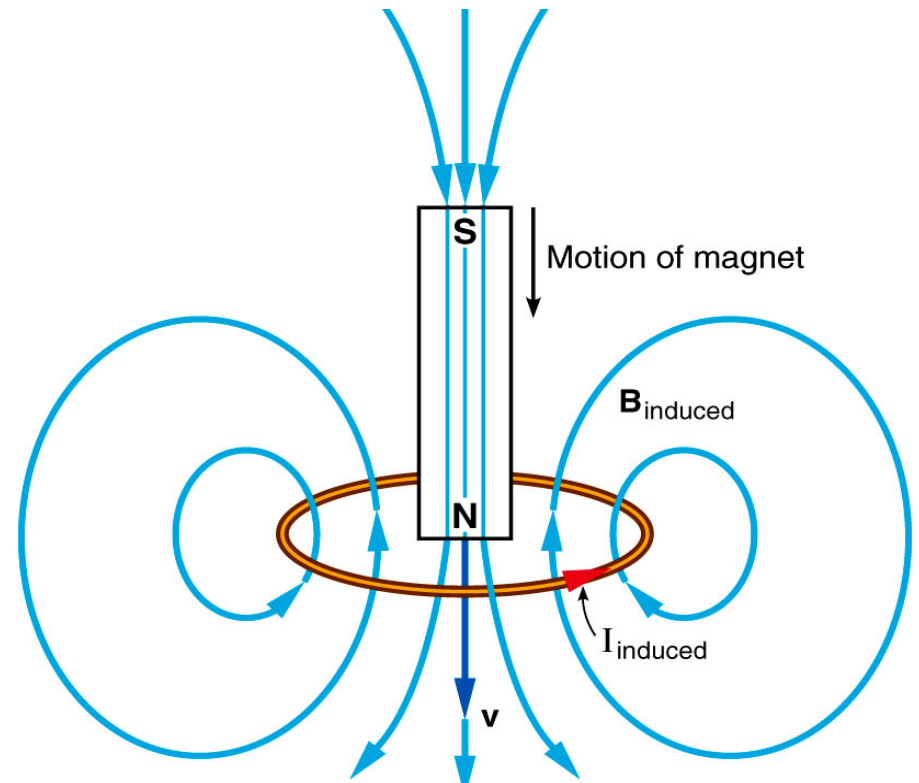
Lenz's Law (19th century):

- ❖ The **direction** of the **induced current** (generated by changing magnetic flux) is such that it produces a **magnetic field** that *opposes* the **changes in original flux**.

E.g. If field **increases** with time the field produced by **induced current** will be **opposite in direction** to original external field (and vice versa).

- As magnet is pushed through coil loop, the **induced field opposes** its field.

Note: This also explains why the **current** meter needle **deflects in opposite directions** when magnet pulled **in** and **out** of **coil** in laboratory demonstration.



Waves (Chapter 15)

Waves are everywhere:

- atmosphere (acoustic)
- oceans (tides)
- land (seismic)
- space (radiation)

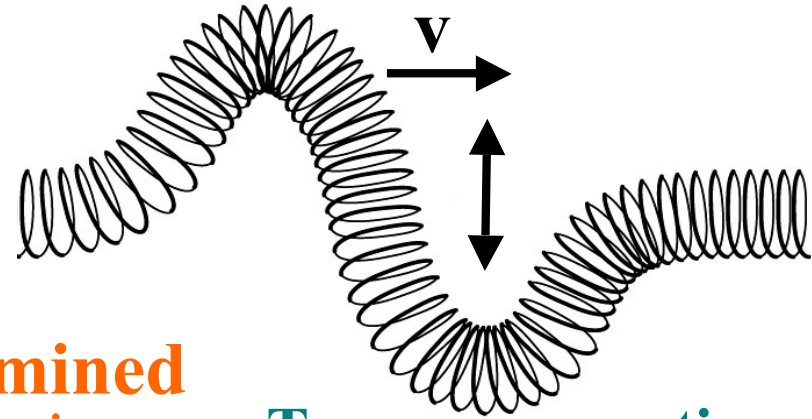
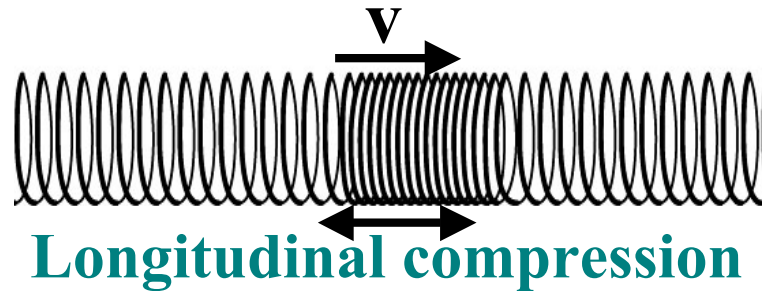
- Waves are **very important mechanism** for the **transport of energy**.
- Wave motions have **implications** in **all areas** of **physics**: an enormous range of phenomena can be explained in terms of waves, from quantum mechanics to tsunamis!

So what is a wave?

Fundamental question: As waves **move** towards the **shore**, why is there **no buildup** of **water** on the beach?

- **Result:** A wave is a **disturbance** that **moves** within a **medium**. (but the medium itself **stays put!**)
- A wave can consist of a **single “pulse”** or a **series of periodic pulses**.

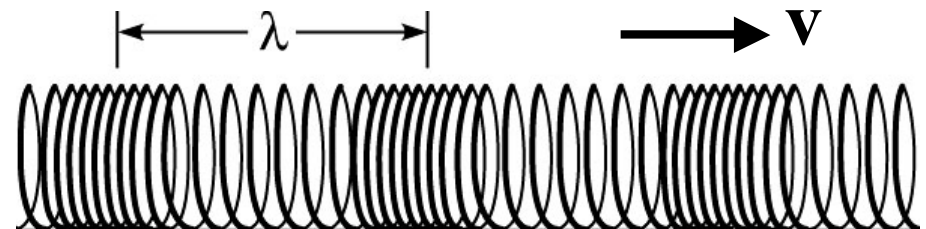
- The **wave disturbance** can be in the form of a:



- **Velocity** of the 'pulse' is **determined** by the **medium** it is propagating in.
- The **wave acts to transmit energy** through the **medium...** (shore line erosion).

Periodic waves:

- A periodic wave consists of a **series of pulses** at **regular (equal) time intervals**.
- Time between the pulses is called the **wave period (T)**.
- **Frequency of wave is number of pulses per second:**

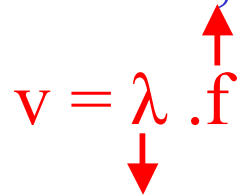


$$f = \frac{1}{T} \quad (\text{Units Hertz, Hz})$$

- **Separation of the pulses** is called the **wavelength** (λ).
- Thus for a **periodic disturbance**, the **velocity** is **equal** to **one wavelength** (i.e. distance between two successful pulses) **divided by one period** (i.e. time between the pulses).

$$v = \frac{\lambda}{T} \quad \text{or} \quad v = \lambda \cdot f$$

- This is valid for **any periodic wave** (sound, light, etc) and relates the **velocity** to **wavelength** and **frequency**.
- The wave **velocity depends** on the properties of the medium (e.g. air, water, ground) and is often known.
- The **wave frequency** is a **property** of the **wave source** (e.g. speech).
- As the **frequency varies**, the **wavelength changes**:

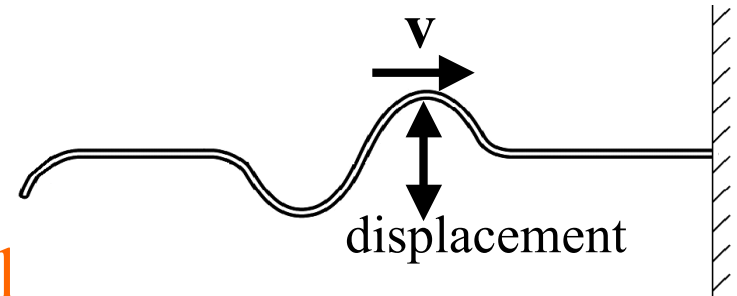
$$v = \lambda \cdot f$$


... to keep velocity constant.

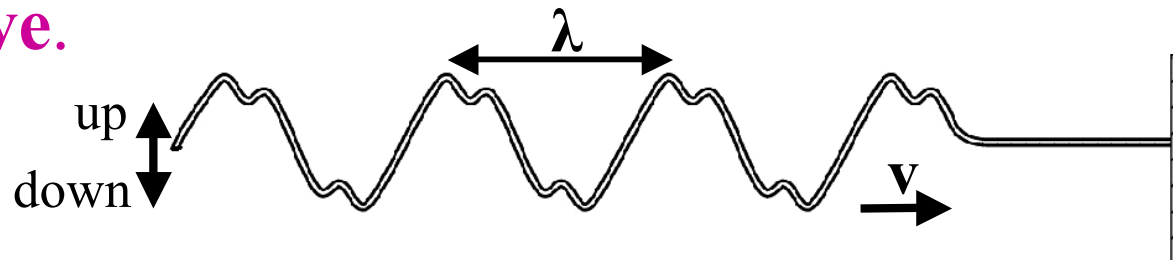
Example: Waves on a Rope

- By moving **free end up and down** we can generate a **transverse wave 'pulse'**.

Pulse propagates down rope to wall creating an instantaneous vertical displacement.

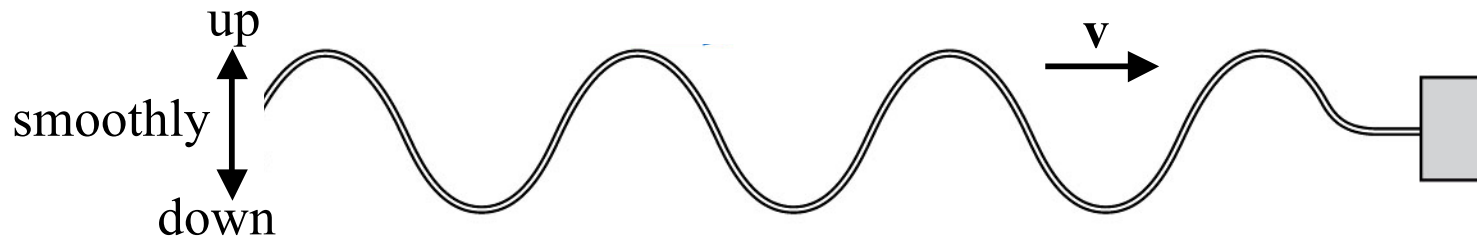


- A series of 'snap-shots' would show the **wave moving down** rope at **constant speed 'v'**.
- If we **repeat up /down motion regularly** you can make a **periodic wave**.



- A **periodic wave** can have a **complex shape** depending on the **perturbation induced**.
- When the **wave reaches the wall**, it is **reflected back** along rope and then **interferes** with the **forward moving wave** creating a **more complex** wave pattern.

Simple Harmonic Wave (Pure Sinusoid)

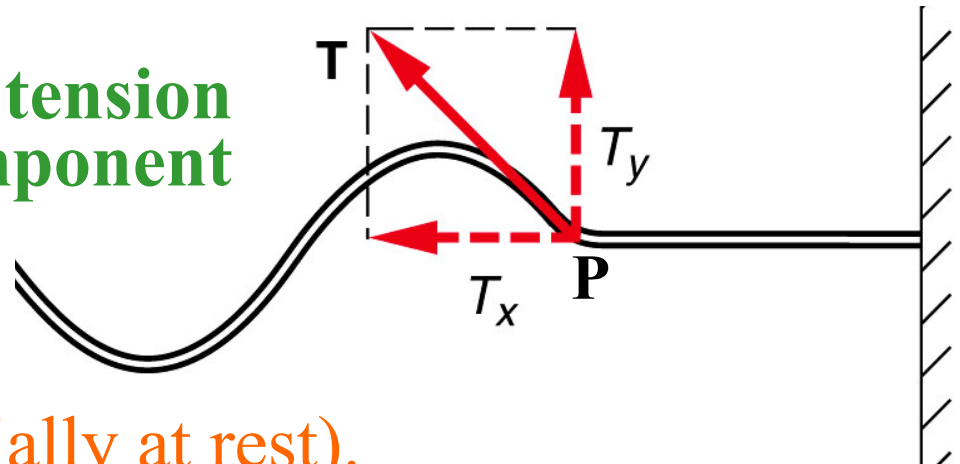


- When we move rope end up and down very **smoothly** and **regularly**, we create a **sinusoidal variation** called a “**harmonic wave**”.
- **Harmonic waves** are **easy to create** as the individual “**elements**” in a **rope** act like a **spring** which is a **natural harmonic oscillator** (Force \propto – displacement).
- **Harmonic waves** are very **important** for **everyday wave analysis** as any **complex periodic wave motion** can be **broken down** into a **sum of pure harmonic waves**.
- **Fourier analysis** – uses harmonic waves as building blocks for complex everyday wave motions (e.g. speech).

Why does the pulse move?

- Experiments show **velocity** is **independent** of wave **shape**.

- **Lifting** the rope causes the **tension** in it to gain an **upward component** of motion.
- This **upward force** acts on **element** of rope to **right** of point 'P' (which was initially at rest).
- This causes the **next element** to **accelerate upwards** and so on down the rope.
- **Velocity of pulse** (wave) depends on how **fast** the **individual elements respond** to the initial **perturbation** (i.e. on how fast they can be **accelerated** by the **tension force**).



$$v = \sqrt{\frac{T}{\mu}} \quad \text{where } \mu = \frac{\text{mass of rope}}{\text{length}}$$

Result (for a rope):

- **Larger tension** => **higher wave velocity**.
- **Heavier rope** (μ larger) => **slower wave speed**.

Example: A rope of length 12 m and total mass 1.2 kg has a tension of 90 N. An oscillation of 5 Hz is induced. Determine velocity of wave and wavelength.

1) First we need to calculate μ :

$$\mu = \frac{m}{L} = \frac{1.2}{12} = 0.1 \text{ kg/m}$$

$$\begin{aligned} L &= 12 \text{ m} \\ m &= 1.2 \text{ kg} \\ T &= 90 \text{ N} \end{aligned}$$

2) now velocity:

$$v = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{90}{0.1}} = \sqrt{900} = 30 \text{ m/s}$$

3) and wavelength:

$$v = f \cdot \lambda \quad \text{or} \quad \lambda = \frac{v}{f}$$

$$\lambda = \frac{30}{5} = 6 \text{ m}$$