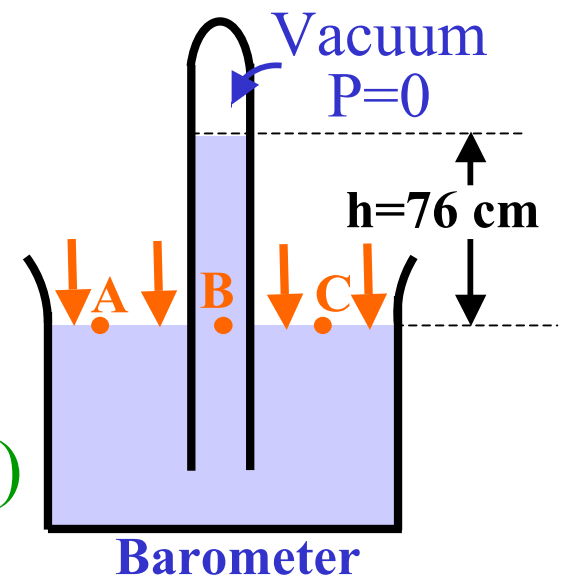


Recap: Pressure

- Pressure = Force per unit area ($P = F / A$; units: Pascals)
- Density of object = mass / volume ($\rho = m / V$; units: kg / m^3)
- **Pascal's Law:** Pressure is transmitted equally in all directions throughout the fluid.
- In a fluid **gravity** is the cause of **hydrostatic pressure** resulting in an **increase in pressure** with depth.

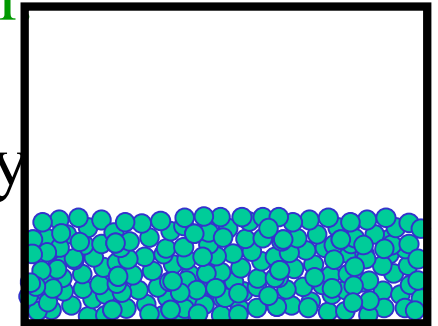
$$\text{Pressure} = \frac{F}{A} = \rho \cdot g \cdot h$$

- Pressure at A,B,C is same: at A, C (weight of atmosphere, at B (weight of mercury).
- Thus the **height of mercury** is a direct **measure of atmospheric pressure**.
- Force due to atmospheric pressure ($\sim 10^5 \text{ Pa}$) is very powerful.

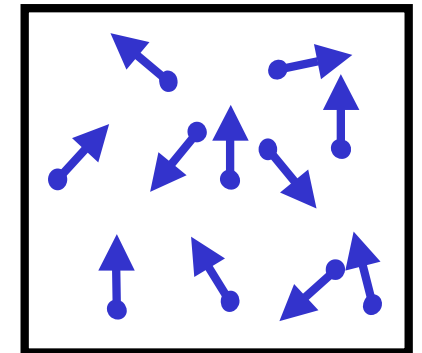


Static Fluids (Chapter 9)

- Most **liquids** are **NOT** readily compressible, so increasing pressure does **NOT** change their **volume** much.
- This is because the **molecules** in a liquid are **closely packed together** (like in a solid) – they cannot easily be squeezed.
- **Density** of a **liquid** therefore stays the **same**.
- **Gases** (e.g. air) are much **easier to compress**. As the **pressure changes the volume changes**.
- Except at very high pressures the **atoms /molecules of a gas** are **separated by large distances** compared to size of atoms.
- The **density** of a **gas** therefore **changes** with pressure.
- **Gases** can also **expand** if the **pressure is reduced**.
- Changes in **temperature** have much **bigger effect** on **gas pressure /volume** than on a **liquid**.



liquid



gas

Boyle's Law (Mariotte's Law) (17th century)

- How does the volume of a gas change with pressure at constant temperature?
- Experiments with “U” shaped tubes containing mercury liquid showed that the **volume** of trapped gas **decreases** as **pressure increases**.

$$P \cdot V = \text{constant}$$

$$\text{or } P_1 \cdot V_1 = P_2 \cdot V_2$$

- So if **pressure increases** the **volume decreases** to keep their **product constant** (at fixed temperature).
- The density (ρ) also changes **inversely** with the volume change ... ($\rho = \text{mass} / \text{volume}$).
- For example, if the volume decreases the density will increase and vice versa.

Examples Using Boyle's Law

Example 1: Increase pressure on a volume of air of 0.5 m^3 from $1 \times 10^5 \text{ Pa}$ (1 atmosphere) to 5 x atmospheric pressure (5 atmospheres) at constant temperature.

$$P_1 \cdot V_1 = P_2 \cdot V_2$$

$$V_2 = \frac{1 \times 0.5}{5} = 0.1 \text{ m}^3 \quad \text{i.e. Volume reduces 5 times}$$

As density $\rho = \frac{m}{V}$ and density **increases** by 5 times.

Example 2: Same volume of air (0.5 m^3) at sea level is allowed to expand (at constant temperature) to height of 10 km where pressure = $26 \times 10^3 \text{ Pa}$.

$$P_1 \cdot V_1 = P_2 \cdot V_2$$

$$V_2 = \frac{0.5 \times (1 \times 10^5)}{26 \times 10^3} = 1.9 \text{ m}^3 \quad \text{(Volume increased)}$$

(Density ρ **decreases** by factor of ~ 4)

Floatation

- **Why** do some objects **float** easily while others **sink**?
 - Does it depend on its weight?
 - What is the effect of objects shape?
- **Answer:** **Density is the key to floatation!**
- Objects whose **average density** is **greater** than the **fluid** they are immersed in will **sink**, but those **less dense** will **float**.
- **Example:** Wood is **less dense** ($\rho = \text{mass} / \text{volume}$) than water and **floats**; steel is **more dense** and it **sinks**!

Buoyancy Force

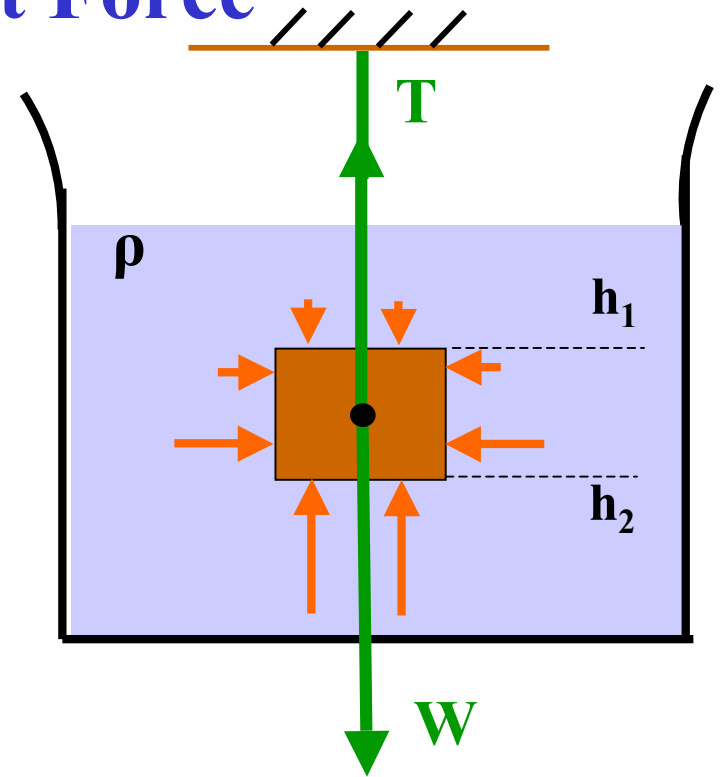
- If you **push down** on a block of **floating wood** you instantly feel a **force pushing back**.
- **Force is large** – very hard to submerge a low density object (e.g. life jacket).
- **The upward force is called Buoyancy Force.**
- The more you **push down** a partially submerged object (e.g. toy duck) the **larger the buoyancy** force response.

Archimedes' Principle

- Archimedes realized what determines the **strength** of the buoyancy force.
- When an object is **submerged** it **takes up space** previously occupied by the **liquid**, i.e. it **displaces** the fluid.
- The **more fluid displaced**, the **greater** the upward **buoyancy force**.
- Once an object is **completely submerged** it cannot **displace any more liquid** and the **buoyancy force** will remain **constant** (with depth change).
- ❖ The **buoyant force** acting on an object (partially or fully) submerged in a fluid is **equal** to the **weight of fluid displaced**.
- An object will therefore **float** if it **displaces** a volume of fluid that is **heavier** than the object.
- i.e. The **buoyant force** is **greater** than **object's weight**...

Origin of Buoyant Force

- The source of the buoyant force is the **change in pressure** with depth.
- **Pressure** acting on **bottom** of block is **larger** than **top** due to increase of pressure with depth
- Results in net **upward** force.



At a given depth: $P = \rho \cdot g \cdot h$

The pressure difference = $\rho \cdot g \cdot \Delta h$ (where $\Delta h = h_2 - h_1$)

Force due to pressure difference = $\rho \cdot g \cdot \underline{\Delta h \cdot A}$ (volume block)

- ❖ **Buoyancy force = $\rho \cdot g \cdot V$ = weight liquid displaced (m.g)**
- The **buoyant force** is therefore dependent on the **density** and **volume** (i.e. **weight**) of **liquid displaced**.

State of Floatation (3 possibilities)

- The **weight of an object** and the resultant **buoyancy force** determine whether it will **float** or **sink**.

1. Density of object greater than fluid density:

- Weight of object is greater than weight of fluid displaced (as volume is same when fully submerged).
- **Net force** (weight – buoyancy) is **downward**; **it sinks!**
- Example: A submarine takes on sea water to replace air and increases its **average density** (i.e. weight) to submerge.

2. Density of object less than fluid density:

- Buoyant force is **larger** than object's **weight** when fully submerged.
- Net force is **upward!** Object will **float** at an **equilibrium level** where **buoyancy force = weight**.

3. Density of object equals that of fluid:

- The weight of object exactly equals the weight of fluid displaced when it is **fully submerged**.

3. Density of object equals that of fluid (cont):

- The object **floats** when **fully submerged**.
- Fish, and submarines exist in this state changing their **average density** slightly to **rise** or **fall** in depth.

Effect of Shape on Floatation

- Metal is much more dense than water but can be made to float by creating a shape /volume whose **average density** is less than water.
- At **equilibrium** (floatation) the **buoyant force equals ships weight**.
- When it takes on **cargo**, the ship will **sink lower** in water (to new **equilibrium position**).
- In a storm if a ship takes on too much **water** its **average density** (and weight) will **increase** and it will **sink** if it exceeds water density.

Floating in the Air

- **Buoyancy** force acts on objects **submerged** in a **gas** e.g. air.
 - If a balloon is filled with a gas whose **density** is **less** than air, (and the **average density** of balloon and gas is **less** than air), then it will **rise**.
 - **Helium gas** (He) is often used (hydrogen too dangerous). Old Zeppelin balloons used **hydrogen** with disastrous consequences.
 - Balloons are made of very **light materials** e.g. mylar (often coated with aluminum).
 - They are **thin, light, strong** and **impermeable** to the gas contained.
- Note:** Helium easily escapes through normal elastic balloon – why they only stay up at children's parties for a day or so...
- **Hot air balloons:** as air expands when heated, it becomes **less dense** and balloon **rises**.
 - A balloon will **rise** until its **average density** equals that of the **surrounding air** (just like a submarine floating in water).

Summary

- **Archimedes' principal** states that the **buoyant force** acting on an object is **equal** to the **weight** of fluid displaced.
- If the **average density** of object is **greater** than density of fluid displaced, the **weight** of object will **exceed buoyant force** and it will **sink** (and vice versa).
- **Buoyancy force** is due to **pressure difference** between **top** and **bottom** of submerged object (as pressure increases with depth).
- **Buoyancy is a very useful force:**
 - Ship floatation; cargo transport.
 - Balloon flights
 - Density determination (irregular shaped objects – Archimedes' original goal).